

1. Show that $\frac{1}{6x^2 + 7x - 5} \div \frac{1}{4x^2 - 1}$ simplifies to $\frac{ax + b}{cx + d}$ where a, b, c and d are integers.

$6x^2 + 7x - 5$

① $6 \times (-5) = -30$

② Find two numbers that multiply to make -30 and add to make 7

$10 \times (-3) = -30$

$10 + (-3) = 7$

Our numbers 10, -3

$(6x + 10)(6x - 3)$

$(3x + 5)(2x - 1)$

try to simplify each bracket

$4x^2 - 1$ ← called difference of two squares

$a^2 - b^2 = (a + b)(a - b)$

$(2x)^2 - (1)^2 = (2x + 1)(2x - 1)$

Factorising quadratics

$6x^2 + 7x - 5 = (3x + 5)(2x - 1)$

$4x^2 - 1 = (2x + 1)(2x - 1)$

$\frac{1}{(3x + 5)(2x - 1)} \div \frac{1}{(2x + 1)(2x - 1)}$

$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \times \frac{d}{c} = \frac{ad}{bc}$

use rule

① $\frac{(2x + 1)(\cancel{2x - 1})}{(3x + 5)(\cancel{2x - 1})} = \frac{2x + 1}{3x + 5}$

$\frac{2x + 1}{3x + 5}$

2. $2 - \frac{x+2}{x-3} - \frac{x-6}{x+3}$ can be written as a single fraction in the form $\frac{ax+b}{x^2-9}$

where a and b are integers.

Work out the value of a and the value of b .

$$\downarrow (x+3)(x-3)$$

$$\begin{aligned} & \frac{2(x^2-9)}{x^2-9} - \frac{(x+2)(x+3)}{x^2-9} - \frac{(x-6)(x-3)}{x^2-9} \quad \textcircled{1} \\ & = \frac{2(x^2-9) - (x+2)(x+3) - (x-6)(x-3)}{x^2-9} \\ & = \frac{(2x^2-18) - (x^2+5x+6) - (x^2-9x+18)}{x^2-9} \quad \textcircled{1} \\ & = \frac{2x^2-18-x^2-5x-6-x^2+9x-18}{x^2-9} = \frac{4x-42}{x^2-9} \end{aligned}$$

$$\boxed{a=4, b=-42.} \quad \textcircled{1}$$

$$a = 4$$

$$b = -42$$

(Total for Question is 4 marks)

3. (a) Simplify $\frac{x^2 - 16}{2x^2 - 5x - 12}$

$$\frac{(x+4)(\cancel{x-4}) \textcircled{1}}{(2x+3)(\cancel{x-4}) \textcircled{1}} = \frac{x+4}{2x+3}$$

$$\textcircled{1} \frac{x+4}{2x+3}$$

(3)

(b) Make v the subject of the formula $w = \frac{15(t-2v)}{v}$

$$w = \frac{15(t-2v)}{v}$$

$$\times v \left(\begin{array}{l} wv = 15(t-2v) \end{array} \right) \times v$$

$$wv = 15t - 30v \textcircled{1}$$

$$wv + 30v = 15t \textcircled{1}$$

$$v(w+30) = 15t$$

$$\div (w+30) \left(\begin{array}{l} v = \frac{15t}{w+30} \end{array} \right) \div (w+30)$$

$$\textcircled{1} v = \frac{15t}{w+30}$$

(3)

(Total for Question **is 6 marks**)

4. (a) Factorise $a^2 - b^2$ Difference of two squares (D.O.T.S)

$$\begin{aligned} (a+b)(a-b) &= a^2 + ab - ab - b^2 \\ &= a^2 - b^2 \end{aligned}$$

$$\frac{(a+b)(a-b)}{(1)}$$

Use information from part a

- (b) Hence, or otherwise, simplify fully $(x^2 + 4)^2 - (x^2 - 2)^2$
 $a^2 - b^2$

$$a = x^2 + 4$$

$$b = x^2 - 2 \quad (1)$$

$$a^2 - b^2 = (a+b)(a-b) \quad \leftarrow \text{Seen in part a}$$

$$= ((x^2 + 4) + (x^2 - 2))((x^2 + 4) - (x^2 - 2)) \quad (1)$$

$$= (2x^2 + 2) \times 6$$

$$= 12x^2 + 12$$

$$= 12(x^2 + 1)$$

$$\frac{12(x^2 + 1)}{(3)}$$

(Total for Question is 4 marks)

5. (a) Simplify $m^3 \times m^4$

Laws of indices

$$x^a \times x^b = x^{a+b}$$

$$m^{3+4} = m^7$$

$$m^7$$

(1)

(b) Simplify $(5np^3)^3$
 $(5 \times n \times p^3)^3$ - raise each individual term to the power of 3.

$$= 5^3 \times n^3 \times (p^3)^3$$

$$= 125 \times n^3 \times p^9$$

$$= 125n^3p^9$$

Laws of Indices
 $(x^a)^b = x^{ab}$

$$(p^3)^3 = p^9$$

① 2 correct terms

$$125n^3p^9$$

(2)

(c) Simplify $\frac{32q^9r^4}{4q^3r}$ = $\frac{32 \times q^9 \times r^4}{4 \times q^3 \times r}$ = $\frac{32}{4} \times \frac{q^9}{q^3} \times \frac{r^4}{r}$

Laws of Indices:

$$\frac{x^a}{x^b} = x^{a-b}$$

$$= 8 \times q^{9-3} \times r^{4-1}$$

$$= 8 \times q^6 \times r^3$$

① 2 correct terms

$$8q^6r^3$$

(2)

(Total for Question is 5 marks)

It is not in line with the trend of the other points.
 doesn't fit trend - far from other points / line of best fit

It is not in line with the trend of the other points.

Extrapolation -> extending graph beyond plotted points is unreliable as we can't be sure that the trend will continue.

The point would be outside of the range of the scatter diagram

6. Expand and simplify $5(p+3) - 2(1-2p)$

$$\begin{aligned} & ((5 \times p) + (5 \times 3)) + (-2 \times 1) + (-2 \times -2p) \\ &= (5p + 15) + (-2 + 4p) \quad \text{① Expanding 1 bracket} \\ &= (5p + 4p) + (15 - 2) \\ &= 9p + 13 \quad \leftarrow (13 \text{ is prime}) \end{aligned}$$

9 and 13 have no common factors,
so this can't be simplified further.

$$9p + 13 \quad \text{①}$$

(Total for Question is 2 marks)

7. (a) Simplify $\left(\frac{1}{m^2}\right)^0$ $a^0 = 1$

$$\frac{1}{\dots\dots\dots}$$

(1)

(b) Simplify $\frac{8(x-4)}{(x-4)^2}$

$$\frac{8\cancel{(x-4)}}{(x-4)\cancel{(x-4)}}$$

$$\frac{8}{x-4}$$

(1)

(c) Simplify $(3n^4w^2)^3$

$$(abc)^n = a^n b^n c^n$$

$$(a^x)^y = a^{xy}$$

$$3^3 (n^4)^3 (w^2)^3 = 27 n^{12} w^6$$

$$\frac{27 n^{12} w^6}{\dots\dots\dots}$$

(2)

(Total for Question is 4 marks)